

# Precalculus Khan Academy Video Correlations By SpringBoard Activity

SB Activity	Video(s)
Unit 1: Sequences, Series, Expo	nential and Logarithmic Functions
Activity 1	Sequences and Subscript Notation
Arithmetic Sequences	Arithmetic sequences
1-1 Learning Targets:	
<ul> <li>Write an expression for a sequence.</li> </ul>	Finding the 100 <sup>th</sup> term in a sequence
<ul> <li>Use subscript notation.</li> </ul>	Equations of sequence patterns
1-2 Learning Targets:	Sigma Notation
<ul> <li>Use sigma notation to represent a series.</li> </ul>	Sigma notation for sums
<ul> <li>Write the algebraic form of an arithmetic</li> </ul>	
sequence.	Mathematical Induction
Calculate the nth term or nth partial sum	Proof by induction
of an arithmetic series.	Alternate proof to induction for integer sum
1-3 Learning Targets:	Attenute proof to madelon for meger sum
<ul> <li>Understand the method of mathematical induction.</li> </ul>	
<ul> <li>Use mathematical induction to prove</li> </ul>	
statements.	
Activity 2	Identifying Geometric Sequences
Geometric Sequences	Geometric sequences introduction
2-1 Learning Targets:	Geometric sequences
Identify a geometric sequence.	
Determine the common ratio of a geometric	Finite Geometric Sequences and Series
sequence.	Geometric series
2-2 Learning Targets:	Formula for a finite geometric series
<ul> <li>Write the algebraic form of a geometric</li> </ul>	Series as sum of sequence
sequence.	Constructing a geometric series for new users
• Calculate the sum of a finite geometric series.	
2-3 Learning Targets:	Geometric series sum to figure out mortgage
Determine if a sequence converges or	<u>payments</u>
diverges.	Infinite Geometric Sequences and Series
• Find the sum of an infinite geometric series.	Sum of an infinite geometric series
	Another derivation of the sum of an infinite geometric series
	Geometric series convergence and divergence examples
	Repeating decimal as infinite geometric series
	Vertical distance of bouncing ball



**Explicit and Recursive Formulas** 

Converting an explicit function to a recursive function

Explicit and recursive definitions of sequences

#### Activity 3

Modeling Recursive Relationships

#### 3-1 Learning Targets:

- Represent arithmetic and geometric sequences recursively.
- Determine the explicit form of a recursive sequence.

#### 3-2 Learning Targets:

- Represent arithmetic and geometric sequences recursively.
- Determine the explicit form of a recursive sequence.

**Exponential growth functions** 

**Graphing exponential functions** 

Solving exponential equation

#### **Activity 4**

**Exponential Functions** 

#### 4-1 Learning Targets:

- Write, graph, analyze, and model with exponential functions.
- Solve exponential equations.

#### 4-2 Learning Targets:

- Write, graph, analyze, and model with exponential functions.
- Calculate compound interest.
- Solve exponential equations.

#### 4-3 Learning Targets:

- Write, graph, analyze, and model with exponential functions.
- Calculate compound interest.
- Solve exponential equations.

Introduction to compound interest and e

Compound interest and e (part 2)

Compound interest and e (part 3)

Compound interest and e (part 4)

#### **Activity 5**

Logarithms

#### 5-1 Learning Targets:

- Explore the inverse relationship between exponents and logarithms.
- Graph logarithmic functions and analyze key features of the graphs.

#### 5-2 Learning Targets:

- Apply the Change of Base Formula.
- Use properties of logarithms to evaluate and transform expressions.

#### 5-3 Learning Targets:

- Solve exponential equations by taking the logarithm of both sides.
- Use properties of exponents and logarithms to solve logarithmic equations.

#### **Common and Natural Logarithms**

**Comparing exponential and logarithmic functions** 

**Graphing logarithmic functions** 

Matching functions to their graphs

**Graphs of logarithmic functions** 

#### Using Properties and the Change of Base Formula

Introduction to logarithm properties

**Introduction to logarithm properties (part 2)** 

Logarithm of a power

Sum of logarithms with same base

Using multiple logarithm properties to simplify

Change of base formula

**Solving Logarithmic Equations** 

### **Exponential Functions and Equations**

### **Modeling with Exponential Functions**

**Exponential growth and decay word problems** 

Decay of cesium 137 example

**Modeling ticket fines with exponential function** 

### **Compound Interest**



	Solving exponential equation with logarithm
	Solving exponential equation
	Solving logarithmic equations
	Solving logarithmic equations
Activity 6	Transforming Functions
Transformations of Functions	Recognizing odd and even functions
6-1 Learning Targets:	Connection between even and odd numbers and
Graph transformations of functions and	<u>functions</u>
write the equations of the transformed functions.	Recognizing features of functions (example 1)
<ul> <li>Describe the symmetry of the graphs of</li> </ul>	Recognizing features of functions (example 2)
even and odd functions.	Recognizing features of functions (example 3)
6-2 Learning Targets:	Function Operations
<ul> <li>Add, subtract, multiply, and divide functions.</li> </ul>	Sum of functions
<ul> <li>Transform and perform operations with</li> </ul>	Difference of functions
piecewise-defined functions.	Product of functions
	Quotient of functions
Activity 7	Finding a regression Line
Modeling with Power Functions	Fitting a line to data
7-1 Learning Targets:	Squared error of regression line
<ul> <li>Write an equation that models a data set.</li> </ul>	Regression line example
Transform data to determine whether a	
power function is a good model for a data	Second regression example
set. 7-2 Learning Targets:	
<ul> <li>Graph power functions.</li> </ul>	
<ul> <li>Identify and analyze key features of the</li> </ul>	
graphs of power functions.	
Activity 8	Composition of Functions
Compositions of Functions and Inverses	Introduction to function composition
8-1 Learning Targets:	Creating new function from composition
<ul> <li>Determine the composition of two functions.</li> </ul>	Evaluating composite functions example
<ul> <li>Determine the inverse of a function.</li> </ul>	Modeling with function composition
	Inverse Functions
8-2 Learning Targets:	Introduction to function inverses
<ul> <li>Find the inverse of a function.</li> <li>Restrict the domain of a function so that</li> </ul>	Function inverse example 1
its inverse is also a function.	Function inverses example 2
its inverse is also a failetion.	Function inverses example 3
Unit 2: Functions	and Their Granhs
Unit 2: Functions and Their Graphs	



Activity 9	Polynomial Functions: End Behavior
Polynomials	Polynomial end behavior
9-1 Learning Targets:	
Compare models to best fit a data set.	Polynomial end behavior example
Use a polynomial regression to make	Another polynomial end behavior example
predictions.	Polynomial end behavior exercise example
9-2 Learning Targets:	
<ul> <li>Describe and analyze graphs of polynomial functions.</li> </ul>	
<ul> <li>Graph polynomial functions using technology.</li> </ul>	
Activity 10	Fundamental Theorem of Algebra
Analyzing Polynomial Functions	Fundamental theorem of algebra
10-1 Learning Targets:	
<ul> <li>Analyze end behavior and zeros to sketch</li> </ul>	Fundamental theorem of algebra for quadratic
polynomial functions.	Factoring Polynomials
Understand the Fundamental Theorem of	Factoring sum of cubes
<ul><li>Algebra.</li><li>Understand the Linear Factorization</li></ul>	Difference of cubes factoring
Theorem.	Factoring special products
10-2 Learning Targets:	Example: Factoring a fourth degree expression
Apply the Rational Root Theorem to find	Roots of Polynomial Functions
zeros.	Possible number of real roots
Use the Factor Theorem.	Identifying graph based on roots
Apply the Remainder Theorem.  10.3 Learning Targets:	
<ul><li>10-3 Learning Targets:</li><li>Use Descartes' Rule of Signs.</li></ul>	
<ul><li> Use Descartes' Rule of Signs.</li><li> Accurately graph polynomial functions.</li></ul>	
Activity 11	Complex Conjugates
Complex Polynomial Roots and Inequalities	Complex conjugates example
11-1 Learning Targets:	
Maximize volume in applications.	Roots of Polynomials  Factoring 5 <sup>th</sup> degree polynomial to find real zeros
<ul> <li>Apply the Complex Conjugate Theorem.</li> </ul>	ractoring 3 degree polynomial to find real zeros
11-2 Learning Targets:	
Rewrite polynomial functions in factored	
form.	
<ul> <li>Find all of the zeros of a polynomial</li> </ul>	
function.	
11-3 Learning Targets:	
<ul> <li>Solve polynomial inequalities.</li> </ul>	
<ul> <li>Represent solutions using interval notation and graphs.</li> </ul>	
Activity 12	Asymptotes
Rational Expressions and the Reciprocal Function	Asymptotes of rational functions
12-1 Learning Targets:	Horizontal and vertical asymptotes of function



Write ratios of variable expressions.	Finding horizontal and vertical asymptotes
<ul> <li>Write a rational function based on a real-</li> </ul>	Rational Functions and Their Gaphs
world scenario.	Matching rational functions to their graphs
12-2 Learning Targets:	
<ul> <li>Write equations for vertical and horizontal</li> </ul>	
asymptotes.	
<ul> <li>Sketch the graph of a rational function.</li> </ul>	
Activity 13	Graphing Rational Functions
Rational Functions	Another rational function graph example
13-1 Learning Targets:	A third example of graphing a rational function
Compare and contrast graphs of rational	
functions.	
Write and sketch graphs of	Rational Inequalities
transformations of rational functions.	Rational inequalities
13-2 Learning Targets:	Rational inequalities 2
Determine horizontal, vertical, or oblique	
asymptotes.	
<ul><li>Accurately graph rational functions.</li><li>Solve rational inequalities.</li></ul>	
13-3 Learning Targets:	
Write the equation of a rational function	
given certain attributes.	
<ul> <li>Solve rational inequalities.</li> </ul>	
	metric Functions
Activity 14	Radian Measure
Angles and Angle Measure	Introduction to radians
14-1 Learning Targets:	Rotation by radians and quadrants
<ul> <li>Draw angles in standard position.</li> </ul>	
• Find the initial side and terminal side of an	Finding arc length from radian angle measure
angle in standard position.	Example: Radian measure and arc length
<ul> <li>Identify coterminal angles.</li> </ul>	Example: Converting degrees to radians
14-2 Learning Targets:	Example: Converting radians to degrees
<ul> <li>Measure angles in radians.</li> </ul>	
<ul> <li>Convert angle measures from degrees to</li> </ul>	Radian and degree conversion practice
radians.	Radians and degrees
<ul> <li>Recognize trigonometric ratios to</li> </ul>	
complete reference triangles.	
Activity 15	Exploring Periodic Data
Sinusoidal Functions	Modeling annual temperature variation with
15-1 Learning Targets:	trigonometry
Recognize situations that involve periodic	Modeling temperature through the day
data.	
	Day length in Alaska
Sketch a graph of periodic data.  15. 3 Learning Targets:	Day length in Alaska
Sketch a graph of periodic data.  15-2 Learning Targets:	Periodic Functions  Midline, amplitude and period of a function



Explore how a change in parameters	Example: Amplitude and period
<ul> <li>affects a graph.</li> <li>Determine the period, amplitude, or phase shift of a periodic function.</li> </ul>	Example: Amplitude and period transformations
	Example: Amplitude and period cosine
15-3 Learning Targets:	transformations
Graph a periodic function with various	Graph of the Sine and Cosine Function
domains.	Example: Graph, domain, and range of sine function
<ul> <li>Compare the graph of y = sin x to periodic graphs.</li> </ul>	Example: Graph of cosine
S. april.	Example: Intersection of sine and cosine
Activity 16	The Unit Circle
Trigonometric Functions and the Unit Circle	Introduction to the unit circle
16-1 Learning Targets:	Unit circle manipulative
<ul><li>Label points on the unit circle.</li><li>Use the unit circle to find trigonometric</li></ul>	Matching ratios to trig functions
values.	Solving triangle in unit circle
16-2 Learning Targets:	Finding trig functions of special angles example
<ul> <li>Define the reciprocal trigonometric functions using the unit circle.</li> </ul>	
<ul> <li>Evaluate all six trigonometric functions for</li> </ul>	Reciprocal Trigonometric Functions
an angle in standard position	Secant (sec), cosecant (csc) and cotangent (cot)
	<u>example</u>
	Example: Using trig to solve for missing information
Activity 17	Trigonometric Graphs
Graphs of the form $y = A \sin[B(x - C)] + D$	Example: Figure out the trig function
17-1 Learning Targets:	Determining the equation of a trig function
<ul> <li>Graph a trigonometric function over a specified interval.</li> </ul>	
Describe how changing parameters affect	
a trigonometric graph	
17-2 Learning Targets:	
Find the amplitude and period of a  trice period function	
<ul><li>trigonometric function.</li><li>Write a trigonometric function given its</li></ul>	
graph.	
Model situations with trigonometric	
functions.	
Activity 18	Tangent Graph
Graphs of Trigonometric Functions	
18-1 Learning Targets:	
Sketch the graphs of csc x, sec x, tan x, and	
cot X.	
<ul> <li>Find the period and locate asymptotes of reciprocal trig functions.</li> </ul>	
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<ul> <li>Determine the domain and range of reciprocal trig functions.</li> <li>18-2 Learning Targets:         <ul> <li>Graph transformations of reciprocal trig functions.</li> <li>Describe how changing parameters affect a trigonometric graph.</li> </ul> </li> <li>Activity 19         <ul> <li>Inverse Trigonometric Functions</li> </ul> </li> <li>19-1 Learning Targets:         <ul> <li>Apply a trigonometric function to a realworld situation.</li> <li>Define and apply the inverse cosine function.</li> </ul> </li> <li>19-2 Learning Targets:         <ul> <li>Relate one-to-one functions to inverse trigonometric functions.</li> <li>Define and apply the inverse sine function.</li> </ul> </li> <li>19-3 Learning Targets:         <ul> <li>Define and apply the inverse tangent function.</li> <li>Find values of inverse trigonometric functions.</li> </ul> </li> </ul>	Inverse Cosine Functions Inverse trig functions: arccos Example: Calculator to evaluate inverse trig function  Inverse Sine Functions Inverse trig functions: arcsin Example: Calculator to evaluate inverse trig function  Inverse Tangent Functions Inverse trig functions: arctan Example: Calculator to evaluate inverse trig function  Modeling with Trigonometric Functions Inverse tan domain and range Inverse tangent scenario Angle of sun with the ground based on shadow Modeling annual temperature variation with trigonometry Applying inverse trig function with model
	N/A  and Trigonometric Applications
Activity 21	Trigonometric Identities
Trigonometric Identities	Pythagorean trig identity from soh cah toa
21-1 Learning Targets:	Pythagorean trig identity from unit circle



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Define the reciprocal and quotient	Using the Pythagorean trig identity
identities.	Simplifying Trigonometric Expressions
<ul> <li>Use and transform the Pythagorean</li> </ul>	Examples using pythagorean identities to simplify
identity.	trigonometric expressions
21-2 Learning Targets:	
<ul> <li>Simplify trigonometric expressions.</li> </ul>	
<ul> <li>Verify trigonometric identities.</li> </ul>	
Activity 22	
Identities and Equations	
22-1 Learning Targets:	
<ul> <li>Use the unit circle to write equivalent</li> </ul>	
trigonometric expressions.	
<ul> <li>Write cofunction identities for sine and</li> </ul>	N/A
cosine.	N/A
22-2 Learning Targets:	
<ul> <li>Use trigonometric identities to solve</li> </ul>	
equations.	
<ul> <li>Solve trigonometric equations by graphing.</li> </ul>	
Activity 23	Exploring Sums of Trig Functions
Multiple Angle Identities	Applying angle addition formula for sin
23-1 Learning Targets:	Angle addition formula with cosine
Model a sound wave with a trigonometric	Another example using angle addition formula with
function.	cosine
Derive an expression for the cosine of a	Sine of non special angle
difference.	
23-2 Learning Targets:	Cosine addition identity example
<ul> <li>Write the sum and difference identities for sine, cosine, and tangent.</li> </ul>	Proof of angle addition formula for sine
<ul> <li>Use sum and difference identities to find</li> </ul>	<u>Proof of angle addition formula for cosine</u>
exact values of a trig function.	Double Angle Formulas
<ul> <li>Derive the double angle and half angle</li> </ul>	Double angle formula for cosine example
identities.	
23-3 Learning Targets:	
<ul> <li>Use trigonometric identities to solve</li> </ul>	
equations.	
<ul> <li>Verify trigonometric identities</li> </ul>	
Activity 24	Law of Cosines
Law of Cosines	Law of cosines
24-1 Learning Targets:	Law of cosines to determine grade
<ul> <li>Use trigonometry to draw and interpret</li> </ul>	
diagrams for a model.	Law of cosines for star distance
	<u>Proof of the law of cosines</u>
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•	Write a trigonometric function for a real-
	world situation

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#### 24-2 Learning Targets:

- Write equations for the Law of Cosines using a standard angle.
- Apply the Law of Cosines in real-world and mathematical situations.

#### Law of Sines

#### **Activity 25**

Law of Sines

25-1 Learning Targets:

- Calculate the bearing of a flight.
- Derive and use the Law of Sines.
- Find unknown sides or angles in oblique triangles.

#### 25-2 Learning Targets:

- Determine the number of distinct triangles given certain criteria.
- Use the Law of Sines to solve triangles with unknown sides or angles.

Law of sines

Law of sines for missing angle

**Proof: Law of sines** 

#### Unit 5: Conics, Parametric Equations, and Vectors

#### Activity 26

Parabola Equations and Graphs

26-1 Learning Targets:

- Define conic sections as intersections of a double-napped cone.
- Relate the locus definition of a parabola to its equation.
- Find the inverse relation for a parabola.

#### 26-2 Learning Targets:

- Find the standard form of a parabola.
- Graph parabolas in the coordinate plane.
- Find the focus, directrix, and axis of symmetry of a parabola.
- Find the equation of a parabola with certain characteristics.

Parabolas and Conic Sections

**Introduction to conic sections** 

#### **Graphs of Parabolas**

**Examples: Graphing and interpreting quadratics** 

**Graphing a parabola with a table of values** 

**Graphing a parabola by finding the roots and vertex** 

**Graphing a parabola using roots and vertex** 

<u>Multiple examples graphing parabolas using roots and</u> vertices

#### **Graphs and Equations of Parabolas**

Parabola vertex and axis of symmetry

Focus and directrix introduction

<u>Using the focus and directrix to find the equation of a</u> parabola

Equation for parabola from focus and directrix

Finding focus and directrix from vertex

Finding the vertex of a parabola example

Ellipses



Activity 27	Conic sections: Intro to ellipses
Ellipses and Hyperbolas	Foci of an ellipse
27-1 Learning Targets:	
<ul> <li>Define and sketch an ellipse.</li> </ul>	Identifying an ellipse from equation
<ul> <li>Determine the equation of an ellipse.</li> </ul>	Hyperbolas
<ul> <li>Graph an ellipse using its characteristics.</li> </ul>	Conic sections: Intro to hyperbolas
27-2 Learning Targets:	Conic sections: Hyperbolas 2
<ul> <li>Define and sketch a hyperbola.</li> </ul>	Conic sections: Hyperbolas 3
<ul> <li>Determine the equation of a hyperbola.</li> </ul>	
<ul> <li>Graph a hyperbola using its characteristics.</li> </ul>	Foci of a hyperbola
27-3 Learning Targets:	Proof: Hyperbola foci
Graph hyperbolas to represent a real-	Identifying a hyperbola from an equation
world problem.	
Use equations of hyperbolas to find	Hyperbola and parabola examples
intersection points.	
Activity 28	Polar Coordinates Polar coordinates 1
Polar Graphs	
<ul><li>28-1 Learning Targets:</li><li>Understand and use the polar grid.</li></ul>	Polar coordinates 2
<ul> <li>Define polar coordinates.</li> </ul>	Polar coordinates 3
<ul> <li>Plot and label points in the polar grid.</li> </ul>	
28-2 Learning Targets:	
<ul> <li>Convert rectangular coordinates to a polar</li> </ul>	
point $(r, \theta)$ .	
<ul> <li>Convert polar coordinates to a rectangular</li> </ul>	
point (x, y).	
28-3 Learning Targets:	
<ul> <li>Express x and y in terms of r and θ.</li> </ul>	
<ul> <li>Sketch polar curves on the polar grid.</li> </ul>	
<ul> <li>Use polar functions to represent real-</li> </ul>	
world situations.	
Activity 29	
Polar Curves and Polar Conics	
29-1 Learning Targets:	
<ul> <li>Sketch graphs represented by polar</li> </ul>	
equations.	
<ul> <li>Compare and contrast polar graphs.</li> </ul>	
<ul> <li>Write equivalent rectangular and polar</li> </ul>	N/A
equations.	
29-2 Learning Targets:	
Convert a polar equation to rectangular	
form.	
Convert a rectangular equation to polar	
form.	



projectile motion.

	pringboard
Describe and sketch graphs of polar	
equations.	
29-3 Learning Targets:	
<ul> <li>Classify different types of polar equations.</li> </ul>	
<ul> <li>Explore patterns in the graphs of polar</li> </ul>	
curves.	
<ul> <li>Predict the resulting graph for a polar equation.</li> </ul>	
equation.	
Activity 30	Parametric Equations
Parametric Equations	Parametric equations 1
30-1 Learning Targets:	Parametric equations 2
Use data points on a grid to write linear	Parametric equations 3
equations.	Parametric equations 4
<ul> <li>Interpret the parameters of an equation in a real-world context.</li> </ul>	raiametric equations 4
<ul> <li>Write rules to describe the position of an</li> </ul>	
object at time t.	
30-2 Learning Targets:	
<ul> <li>Define and write parametric equations.</li> </ul>	
Use parametric equations to solve real-	
world problems.	
30-3 Learning Targets:	
<ul> <li>Convert equations from rectangular to</li> </ul>	
parametric, and vice versa.	
<ul> <li>Use parametric equations to solve real-</li> </ul>	
world problems.	
Activity 31	Parametric Equations
Parametric Equations Revisited	Parametric equations 1
31-1 Learning Targets:	Parametric equations 2
<ul> <li>Understand, calculate, and compare angular and linear velocities.</li> </ul>	Parametric equations 3
<ul> <li>Write equations to model circular motion.</li> </ul>	Parametric equations 4
Sketch the graph of circular motion.	
31-2 Learning Targets:	
<ul> <li>Sketch the graph of a moving object.</li> </ul>	
Write parametric equations using	
trigonometry.	
<ul> <li>Use technology to model motion.</li> </ul>	
31-3 Learning Targets:	
<ul> <li>Understand and apply the equations for</li> </ul>	
projectile motion.	
<ul> <li>Write and graph parametric equations.</li> </ul>	
Solve real-world problems involving	



#### **Activity 32**

**Vectors and Complex Numbers** 

#### 32-1 Learning Targets:

- Understand and model rectilinear motion.
- Define and use vectors.
- Use the notation for position vectors.

#### 32-2 Learning Targets:

- Understand and model rectilinear motion.
- Define and use vectors.
- Use the notation for position vectors.

#### 32-3 Learning Targets:

- Find the direction angle of a vector.
- Resolve a vector into its components.
- Sketch vectors and vector sums in the coordinate plane

#### 32-4 Learning Targets:

- Represent complex numbers as vectors.
- Find the conjugate of a complex number.
- Add, subtract, multiply, and divide complex numbers.

#### 32-5 Learning Targets:

- Find the polar form of a complex number.
- Represent complex numbers in polar form in the complex plane.

#### **Introduction to Vectors**

**Vector representations exercise example** 

**Classifying vectors and quantities example** 

#### **Operations with Vectors**

Multiplying a vector by a scalar

**Visualizing vector addition examples** 

**Adding vectors** 

**Adding vectors exercise example** 

**Subtracting vectors exercise example** 

#### **Vector Components**

**Breaking down vectors into components** 

Magnitude and direction of vector sums

**Magnitude of vector sums** 

#### **Complex Numbers and Operations**

**Introduction to complex numbers** 

Plotting complex numbers on the complex plane

**Adding complex numbers** 

**Subtracting complex numbers** 

**Multiplying complex numbers** 

**Dividing complex numbers** 

#### Polar Form

Complex number polar form intuition exercise

Rectangular to polar form of complex number

#### **Activity 33**

**Applications of Vectors** 

#### 33-1 Learning Targets:

- Write equations to describe rectilinear motion.
- Use vectors to describe velocity of an object.
- Interpret speed as the magnitude of a velocity vector.

#### 33-2 Learning Targets:

- Use vectors to describe planar motion.
- Graph position vectors in the coordinate plane.
- Write a vector equation to model a realworld context.

N/A

Unit 6: Matrices, Systems of Equations, and Volume



#### **Activity 34** Representing Data with Matrices Introduction to the matrix **Matrix Operations** 34-1 Learning Targets: **Representing data with matrices** Use matrices to represent numeric data. **Matrix addition and subtraction** Add and subtract matrices. **Scalar multiplication** • Define and use scalar multiplication. 34-2 Learning Targets: **Matrix Multiplication** • Determine if two matrices can be **Matrix multiplication introduction** multiplied. Multiplying a matrix by a matrix • Find the matrix product of two matrices. Defined and undefined matrix operations Explore properties of matrix operations. 34-3 Learning Targets: **Inverse Matrices** Determine if a matrix has an inverse. Finding the determinant of a 2x2 matrix Find the determinant and inverse of a Inverse of a 2x2 matrix matrix. **Idea behind inverting a 2x2 matrix** • Justify properties of matrix operations. Finding the determinant of a 3x3 matrix method 1 Finding the determinant of a 3x3 matrix method 2 **Linear Transformations Activity 35** Linear transformation examples: Scaling and Matrices and Transformations reflections 35-1 Learning Targets: • Use matrices as vectors to translate figures **Linear transformation examples: Rotations in R2** in the plane. Use matrices as vectors to reflect figures in the plane. 35-2 Learning Targets: • Use matrices as vectors to rotate figures in the plane. • Use matrices as vectors to dilate figures in the plane. 35-3 Learning Targets: Work with matrices to represent realworld situations. Interpret absolute value of determinants as areas. **Activity 36 Matrices and Systems of Equations** Matrices and Systems of Equations Matrices to solve a system of equations 36-1 Learning Targets: **Matrix equations and systems** Write a linear system of equations as a matrix equation.

Represent a real-world situation with a

Identify the coefficient matrix, variable

matrix, and constant matrix.

matrix equation.



#### 36-2 Learning Targets:

- Use an inverse matrix to solve a matrix equation.
- Connect the existence of an inverse matrix to solutions of systems.

#### 36-3 Learning Targets:

- Use technology to solve large linear systems.
- Solve a 3 × 3 matrix equation using technology.

#### **Activity 37**

#### Volume

#### 37-1 Learning Targets:

- Understand Cavalieri's Principle.
- Relate Cavalieri's Principle to volume formulas.

#### 37-2 Learning Targets:

- Informally derive the formula for the volume of a sphere.
- Use volume formulas to solve real-world problems.

#### 37-3 Learning Targets:

- Informally derive the formula for the volume of a sphere.
- Understand the concept of a limit.
- Represent a volume using sums and limits

#### **Volume of Spheres**

#### Volume of a sphere

#### Limits

**Introduction to limits** 

Limit examples (part 1)

**Limit examples (part 2)** 

**Limit examples (part 3)**